

Case B: W/PH is on the upward part of the supply and W/PL is on the vertical portion.
 $W/PH < W_k$ and $W_k = \text{or} < W/PL < W_c$, so $L = L_o$.

It is easily verified that in Case A, holding M_e constant and reducing ML , W is decreased.
 limit to how low ML can be and still be in Case A is when $W/PL = W_k$.

For values of ML less than this critical value, the model changes regime to Case B, as long
 lower values of PL are such that W/PL are $< \text{or} = W_c$, the competitive market clearing
 wage.

For values of ML less than this second critical value of ML , the model changes regime to (

$$E\Pi(X) := (X) \cdot \left[(L_o)^{(\theta)} - \frac{W}{PL} \cdot L_o \right] + (1 - X) \cdot \left[\left(\frac{W}{PH(X)} \right)^{(\theta \cdot \psi)} - \frac{W}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^\psi \right]$$

$$\frac{d}{dW} E\Pi(X) \rightarrow \frac{-X}{PL} \cdot L_o + (1 - X) \cdot \left[\left(\frac{W}{PH(X)} \right)^{\theta \cdot \psi} \cdot \theta \cdot \frac{\psi}{W} - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^\psi - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^\psi \right]$$

$$0 = \frac{d}{dW} E\Pi(X) \text{ solve, } W \rightarrow$$

This generates "no solution was found" because the
 optimal wage is at the boundry where $W_k = W/PL$. The
 first term is neg. In order to verify this differentiate the la
 term.

$$\frac{d}{dW} \left[\left(\frac{W}{PH(X)} \right)^{\theta \cdot \psi} \cdot \theta \cdot \frac{\psi}{W} - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^\psi - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^\psi \cdot \psi \right] \rightarrow \left(\frac{W}{PH(X)} \right)^\theta$$

Because $\theta \cdot \psi < 1$ this must be negative for all W . Consider that Case A is generated by low M 's "clos
 lower values ML are chosen, then the opt. W in Case A become larger until the point when $W/PL = W_k$
 critical value the opt.nominal wage will not change so long as Case B applies, but the real wage W/P
 generate lower and lower values of PL . I will solve for the critical value of ML and Thereby detremine

Again solve (19) and (20) for PL in terms of ML and W and PH in terms of MH and W , and
 substute into the opt. W equ. above. For $X = .2$

$$\begin{aligned}
 X &:= .2 \\
 Y &:= (1-k) \cdot \frac{M}{P} & Y &:= \left(\frac{W}{P}\right)^{(\theta \cdot \psi)} & PH &:= \left[(1-k) \cdot MH \cdot W^{-(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}} \\
 Lo &:= .5 & PL &:= (1-k) \cdot ML \cdot Lo^{-\theta} \\
 k &:= .5 & \theta &:= .6 & \psi &:= .9 & wk &:= (Lo)^{\frac{1}{\psi}} \\
 ML &:= 3.415 & Me &:= 3.685 & MH(X) &:= \frac{(Me - X \cdot ML)}{(1 - X)} & YL &:= Lo^{\theta} & wk &= 0.463
 \end{aligned}$$

$$MH(X) = 3.752$$

This is the solution for case A at the lower bound where regimes shift. We verify that this occurs at $ML = 3.41$.

$$\begin{aligned}
 f(W) &:= W - \exp \left[\ln \left[- (1 + \psi) \cdot \frac{-X \cdot \left[(1-k) \cdot \frac{MH(X)}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}} \cdot \exp \left[\psi \cdot \ln \left[\frac{(1-k) \cdot \frac{M}{W}}{(1-k) \cdot \frac{1}{W}} \right]}{\psi \cdot \theta \cdot \left[(1-k) \cdot \frac{MH(X)}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}} \right]} \right] \right]
 \end{aligned}$$

$$\text{root}(f(W), W) = 1.198$$

$$W := \text{root}(f(W), W) \quad W = 1.198$$

$$PL := (1-k) \cdot ML \cdot Lo^{-\theta}$$

PL varies directly with ML in case B. But at this critical value of ML the same value of PL is generated as when

$$PH(X) := \left[(1-k) \cdot \frac{MH(X)}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}$$

$$PL = \left[(1-k) \cdot \frac{ML}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}$$

$$PH(X) = 3.177 \quad PL = 2.588 \quad Pe := X \cdot PL + (1 - X) \cdot PH(X)$$

$$Pe = 3.059$$

$$wc := \theta \cdot Lo^{(\theta-1)} \quad \frac{W}{Pe} = 0.392 \quad W = 1.198$$

$$\frac{1}{wk} := (Lo)^\psi \quad wc = 0.792 \quad \frac{W}{PH(X)} = 0.377$$

$$wk = 0.463 \quad \frac{W}{PL} = 0.463$$

I verified that for $X = .2$ that the choice of $ML = 3.415$ and $Me = 3.685$ will generate $W/PL = wk$ and that the opt. nominal wage is $W = 1.196$ in Case B. for all values of $ML < 3.415$. $X = .001$ is only of interest in case A as a benchmark for the det. case.

$$LH(X) := \left[(1 - k) \cdot \frac{MH(X)}{PH(X)} \right]^{\frac{1}{\theta}} \quad LH(X) := \left(\frac{W}{PH(X)} \right)^\psi \quad LL := \left(\frac{W}{PL} \right)^\psi$$

$$LH(X) = 0.416 \quad LL = 0.500$$

$$YH(X) := (1 - k) \cdot \frac{MH(X)}{PH(X)} \quad YL := (1 - k) \cdot \frac{ML}{PL} \quad LH(X)^\theta = 0.591$$

$$YH(X) = 0.591 \quad YL = 0.660 \quad LL^\theta = 0.660$$

The

is as the
 will

Case C.

$$\left[\frac{W}{PH(X)} \right]^{\psi} \cdot \psi$$

$$\theta^{\psi} \cdot \frac{\psi^2}{W^2} - \left(\frac{W}{PH(X)} \right)^{\theta \cdot \psi} \cdot \theta \cdot \frac{\psi}{W^2} - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^{\psi} \cdot \frac{\psi}{W} - \frac{1}{PH(X)} \cdot \left(\frac{W}{PH(X)} \right)^{\psi} \cdot \frac{\psi^2}{W}$$

is" to Me. Holding Me constant, as lower and
 is reached. For value of ML lower than this
 L will increase as ML continues to decrease and
 the value of W for Case B.

$$\frac{\left[\frac{H(X)}{(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}}}{\left[\frac{ML}{(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}}} - \left[(1-k) \cdot \frac{ML}{W(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}} + \left[(1-k) \cdot \frac{ML}{W(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}} \cdot X$$

$$\left[X \cdot \exp \theta \cdot \psi \cdot \ln \left[\frac{\left[(1-k) \cdot \frac{MH(X)}{W(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}}}{\left[(1-k) \cdot \frac{ML}{W(\theta \cdot \psi)} \right]^{\frac{1}{(1-\theta \cdot \psi)}}} + 1 - X \right] \right] - \psi \cdot \ln$$

$-1 - \psi + \theta \cdot \psi$

$$\left[\frac{\left[(1-k) \cdot \frac{MH(X)}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}}{\left[(1-k) \cdot \frac{ML}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}} + \theta \cdot \psi \cdot \ln \left[\frac{\left[(1-k) \cdot \frac{MH(X)}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}}{\left[(1-k) \cdot \frac{ML}{W^{(\theta \cdot \psi)}} \right]^{\frac{1}{(1-\theta \cdot \psi)}}} \right] \right] \cdot \left[(1-k) \cdot \frac{ML}{W^{(\theta \cdot \psi)}} \right]$$

$$\frac{1}{(1-\theta \cdot \psi)}$$